# Readington Township Public Schools 

# Algebra 1 <br> (Honors 7th and Advanced 8th) 

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## I. OVERVIEW

This full-year Algebra 1 course is designed to provide Advanced 8 thgrade and Honors $7^{\text {th }}$ grade students with the opportunity to be introduced to algebra skills in the areas of linear, exponential, and quadratic functions, while extending their content base and knowledge to include solving, writing and graphing inequalities, solving systems of equations and inequalities, solving exponential equations, simplifying and factoring higher-degree polynomial functions, graphing and solving quadratic equations, simplifying and solving rational exponents and radical functions, calculating probability, and interpreting data analysis and statistics.

In addition to these topics, and in keeping with the New Jersey Student Learning Standards, students will experience the course content as an integrated, useful, and coherent whole, continually refining their abilities to model with mathematics, reason abstractly and quantitatively while attending to precision both in calculations and vocabulary, and to make sense of problem situations as an essential part of the solution process.

## II. STUDENT OUTCOMES (Linked to New Jersey Student Learning Standards for Mathematics)

## Solve equations and inequalities in one variable.

NJSLS.MATH.CONTENT.HSA.REI.B. 3
Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters.
NJSLS.MATH.CONTENT.HSA.REI.B. 4
Solve quadratic equations in one variable.
NJSLS.MATH.CONTENT.HSA.REI.B.4.A
Use the method of completing the square to transform any quadratic equation in $x$ into an equation of the form
$(x-p)^{2}=q$ that has the same solutions. Derive the quadratic formula from this form.
NJSLS.MATH.CONTENT.HSA.REI.B.4.B
Solve quadratic equations by inspection (e.g., for $x^{2}=49$ ), taking square roots, completing the square, the quadratic formula and factoring, as appropriate to the initial form of the equation. Recognize when the quadratic formula gives complex solutions and write them as $a \pm b i$ for real numbers $a$ and $b$.

## Understand solving equations as a process of reasoning and explain the reasoning.

NJSLS.MATH.CONTENT.HSA.REI.A. 1
Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.
NJSLS.MATH.CONTENT.HSA.REI.A. 2
Solve simple rational and radical equations in one variable, and give examples showing how extraneous solutions may arise.

## Create equations that describe numbers or relationships.

NJSLS.MATH.CONTENT.HSA.CED.A. 1
Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.

## NJSLS.MATH.CONTENT.HSA.CED.A. 2

Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.
NJSLS.MATH.CONTENT.HSA.CED.A. 3
Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context. For example, represent inequalities describing nutritional and cost constraints on combinations of different foods.

## NJSLS.MATH.CONTENT.HSA.CED.A. 4

Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations. For example, rearrange Ohm's law $V=I R$ to highlight resistance $R$.

## Represent and solve equations and inequalities graphically.

NJSLS.MATH.CONTENT.HSA.REI.D. 10
Understand that the graph of an equation in two variables is the set of all its solutions plotted in the coordinate plane, often forming a curve (which could be a line).
NJSLS.MATH.CONTENT.HSA.REI.D. 11
Explain why the $x$-coordinates of the points where the graphs of the equations $y=f(x)$ and $y=g(x)$ intersect are the solutions of the equation $f(x)=g(x)$; find the solutions approximately, e.g., using technology to graph the functions, make tables of values, or find successive approximations. Include cases where $f(x)$ and/or $g(x)$ are linear, polynomial, rational, absolute value, exponential, and logarithmic functions.

## NJSLS.MATH.CONTENT.HSA.REI.D. 12

Graph the solutions to a linear inequality in two variables as a half-plane (excluding the boundary in the case of a strict inequality), and graph the solution set to a system of linear inequalities in two variables as the intersection of the corresponding half-planes.

## Solve systems of equations.

## NJSLS.MATH.CONTENT.HSA.REI.C. 5

Prove that, given a system of two equations in two variables, replacing one equation by the sum of that equation and a multiple of the other produces a system with the same solutions.

## NJSLS.MATH.CONTENT.HSA.REI.C. 6

Solve systems of linear equations exactly and approximately (e.g., with graphs), focusing on pairs of linear equations in two variables.

## NJSLS.MATH.CONTENT.HSA.REI.C. 7

Solve a simple system consisting of a linear equation and a quadratic equation in two variables algebraically and graphically. For example, find the points of intersection between the line $y=-3 x$ and the circle $x^{2}+y^{2}=3$.
NJSLS.MATH.CONTENT.HSA.REI.C. 8
$(+)$ Represent a system of linear equations as a single matrix equation in a vector variable.
NJSLS.MATH.CONTENT.HSA.REI.C. 9
$(+)$ Find the inverse of a matrix if it exists and use it to solve systems of linear equations (using technology for matrices of dimension $3 \times 3$ or greater).

## Interpret the structure of expressions. <br> NJSLS.MATH.CONTENT.HSA.SSE.A. 1

Interpret expressions that represent a quantity in terms of its context.
NJSLS.MATH.CONTENT.HSA.SSE.A.1.A
Interpret parts of an expression, such as terms, factors, and coefficients.
NJSLS.MATH.CONTENT.HSA.SSE.A.1.B
Interpret complicated expressions by viewing one or more of their parts as a single entity. For example, interpret $P(1+r)^{n}$ as the product of $P$ and a factor not depending on $P$.
NJSLS.MATH.CONTENT.HSA.SSE.A. 2
Use the structure of an expression to identify ways to rewrite it. For example, see $x^{4}-y^{4} a s\left(x^{2}\right)^{2}-\left(y^{2}\right)^{2}$, thus recognizing it as a difference of squares that can be factored as $\left(x^{2}-y^{2}\right)\left(x^{2}+y^{2}\right)$.

## Perform arithmetic operations on polynomials.

NJSLS.MATH.CONTENT.HSA.APR.A. 1
Understand that polynomials form a system analogous to the integers, namely, they are closed under the operations of addition, subtraction, and multiplication; add, subtract, and multiply polynomials.

## Understand the relationship between zeros and factors of polynomials.

NJSLS.MATH.CONTENT.HSA.APR.B. 2
Know and apply the Remainder Theorem: For a polynomial $p(x)$ and a number $a$, the remainder on division by $x$ $a$ is $p(a)$, so $p(a)=0$ if and only if $(x-a)$ is a factor of $p(x)$.

Identify zeros of polynomials when suitable factorizations are available, and use the zeros to construct a rough graph of the function defined by the polynomial.

## Use polynomial identities to solve problems.

NJSLS.MATH.CONTENT.HSA.APR.C. 4
Prove polynomial identities and use them to describe numerical relationships. For example, the polynomial identity $\left(x^{2}+y^{2}\right)^{2}=\left(x^{2}-y^{2}\right)^{2}+(2 x y)^{2}$ can be used to generate Pythagorean triples.
NJSLS.MATH.CONTENT.HSA.APR.C. 5
$(+)$ Know and apply the Binomial Theorem for the expansion of $(x+y)^{n}$ in powers of $x$ and $y$ for a positive integer $n$, where $x$ and $y$ are any numbers, with coefficients determined for example by Pascal's Triangle. ${ }^{1}$

## Write expressions in equivalent forms to solve problems.

## NJSLS.MATH.CONTENT.HSA.SSE.B. 3

Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression.
NJSLS.MATH.CONTENT.HSA.SSE.B.3.A
Factor a quadratic expression to reveal the zeros of the function it defines.
NJSLS.MATH.CONTENT.HSA.SSE.B.3.B
Complete the square in a quadratic expression to reveal the maximum or minimum value of the function it defines.
NJSLS.MATH.CONTENT.HSA.SSE.B.3.C
Use the properties of exponents to transform expressions for exponential functions. For example the expression $1.15^{t}$ can be rewritten as $\left(1.15^{1 / 12}\right)^{12 t} \approx 1.012^{12 t}$ to reveal the approximate equivalent monthly interest rate if the annual rate is 15\%.
NJSLS.MATH.CONTENT.HSA.SSE.B. 4 Derive and/or explain the formula for the sum of a finite geometric series (when the common ratio is not 1), and use the formula to solve problems. For example, calculate mortgage payments.*

## Rewrite rational expressions.

NJSLS.MATH.CONTENT.HSA.APR.D. 6
Rewrite simple rational expressions in different forms; write ${ }^{a(x)} / b(x)$ in the form $q(x)+r(x) / b(x)$, where $a(x), b(x), q(x)$, and $r(x)$ are polynomials with the degree of $r(x)$ less than the degree of $b(x)$, using inspection, long division, or, for the more complicated examples, a computer algebra system.
NJSLS.MATH.CONTENT.HSA.APR.D. 7
$(+)$ Understand that rational expressions form a system analogous to the rational numbers, closed under addition, subtraction, multiplication, and division by a nonzero rational expression; add, subtract, multiply, and divide rational expressions.

## III. ESSENTIAL QUESTIONS AND CONTENT

## Reasoning With Equations and Inequalities

What can we do with a system of equations/inequalities that we cannot do with a single equation/inequality?

- Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.
- Solve simple rational and radical equations in one variable, and give examples showing how extraneous solutions may arise.
- Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters.
- Solve quadratic equations in one variable.
- Prove that, given a system of two equations in two variables, replacing one equation by the sum of that equation and a multiple of the other produces a system with the same solutions.
- Solve systems of linear equations exactly and approximately, focusing on pairs of linear equations in two variables.
- Solve a simple system consisting of a linear equation and a quadratic equation in two variables algebraically and graphically.
- Represent a system of linear equations as a single matrix equation in a vector variable.
- Find the inverse of a matrix if it exists and use it to solve systems of linear equations.
- Understand that the graph of an equation in two variables is the set of all its solutions plotted in the coordinate plane, often forming a curve.
- Explain why the x-coordinates of the points where the graphs of two equations intersect are the solutions of the equation when both are set equal.
- Graph the solutions to a linear inequality in two variables as a half-plane and graph the solution set to a system of linear inequalities in two variables as the intersection of the corresponding half-planes.


## Creating Equations

## How do we create equations to represent what we see in the real world?

- Create equations and inequalities in one variable and use them to solve problems.
- Create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales.
- Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in modeling context.
- Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations.


## Seeing Structure in Expressions and Writing Equivalent Forms

## Why do we need to use exponential notation to model situations?

Why should we factor?

## How does the graph of a quadratic function relate to its algebraic equation?

- Interpret and understand the parts of an expression, such as the terms, factors, and coefficients.
- Interpret complicated expressions by viewing one or more of their parts as a single entity. (i.e. P(1+r) as the product of P and a factor not depending on P ).
- Using the structure of an expression and properties of operations to rewrite the expression in a different form.
- Choose and produce an equivalent form of an expression to reveal and explain properties of the quantity represented by the expression.
- Factor a quadratic expression to reveal the zeros of the function it defines.
- Complete the square in a quadratic expression to reveal the max or min value of the function it defines.
- Use the properties of exponents to transform expressions for exponential functions.
- Derive the formula for the sum of a finite geometric


## Arithmetic with Polynomial, Rational, and Radical Expressions

How are rational and irrational numbers the same and different?
Why should we solve rational equations?

- Understand that polynomials form a system analogous to the integers, namely, they are closed under the operations of addition, subtraction, and multiplication.
- Know and apply the Remainder Theorem: For a polynomial $p(x)$ and a number a, the remainder on division by $x-a$ is $p(a)$, so $p(a)=0$ if and only if $(x-a)$ is a factor of $p(x)$.
- Identify zeros of polynomials when suitable factorizations are available, and use the zeroes to construct a rough graph of the function defined by the polynomial.
- Prove polynomial identities and use them to describe numerical relationships.
- Know and apply the Binomial Theorem for the expansion of $(x+y)^{\wedge} n$ in powers of $x$ and $y$ for a positive integer $n$, where $x$ and $y$ are any numbers, with coefficients determined for example by Pascal's Triangle.
- Rewrite simple rational expressions in different forms using inspection, long division, or, for the more complicated examples, a computer algebra system.
- Understand that rational expressions form a system analogous to the rational numbers, closed under addition, subtraction, multiplication, and division by a nonzero rational expression.
IV. STRATEGIES

Intellectual engagement and active involvement of students in daily lessons will be achieved by a variety of teaching strategies, including but not limited to:

- Comprehensive direct instruction utilizing Interactive SMARTBoard technology
- Guided practice using worked-out study examples
- Independent Practice using 'Now You Try' examples
- Student presentation of work/solutions, with explanation and justification of solutions
- High-level questioning and encouragement of student participation
- Student group discussion and mutual help as part of point 3 above
- Regular written 'check for understanding' assessments
- End of unit formative assessments to check for PARCC readiness and to guide instructional choices


## V. EVALUATION

- Chapter Quizzes and Tests
- Final Exam
- Class Participation
- Homework Assignments
- Individual-lesson and unit-based formative assessments


## VI. REQUIRED RESOURCES

## Textbook for course:

McDougal Littell Algebra 1. Larson, R., Boswell, L., Kanold, T.D., \& Stiff, L. Copyright 2004 by McDougal Littell, a Houghton Mifflin Company, Evanston, IL.

## Supplemental resources for course:

Chapter Resource Books. Larson, R., Boswell, L., Kanold, T.D., \& Stiff, L. Copyright 2001 by McDougal Littell, a Houghton Mifflin Company, Evanston, IL.

Standardized Test Practice Workbook. Larson, R., Boswell, L., Kanold, T.D., \& Stiff, L. Copyright 2001 by McDougal Littell, a Houghton Mifflin Company, Evanston, IL.

Big Ideas MATH Algebra 1, Larson, R., Boswell, L. Copyright 2015 by Big Ideas Learning, LLC.

## Suggested supplemental companion Web sites:

McDougal Littell eEdition Plus Online (online textbook: www.classzone.com)
Online Courses including Algebra 1: www.shmoop.com/common-core-standards/
Math problems explained in detail with corresponding NJSLSM references :
www.illustrativemathematics.org
Learnzillion video tutorials: https://learnzillion.com/
Khan Academy video tutorials: www.khanacademy.org
Gizmos

## VII. SCOPE AND SEQUENCE

A. Expressions, Equations, and Functions (5 days)

1. Apply Order of Operations
2. Write Expressions
3. Represent Functions as Rules and Tables
4. Represent Functions as Graphs
B. Properties of Real Numbers (5 days)
5. Use Integers and Rational Numbers
6. Add, Subtract, Multiply, and Divide Real Numbers
7. Apply the Distributive Property
8. Find Square Roots and Compare Real Numbers
C. Solving Linear Equations (15 days)
9. Solve One-Step Equations
10. Solve Two-Step Equations
11. Solve Multi-Step Equations
12. Solve Equations with Variables on Both Sides
13. Write Ratios and Proportions
14. Solve Proportions Using Cross Products
15. Solve Percent Problems
16. Rewrite Equations and Formulas
D. Graphing Linear Equations and Functions (15 days)
17. Graph Linear Equations
18. Graph Using Intercepts
19. Find Slope and Rate of Change
20. Graph Using Slope-Intercept Form
21. Model Direct Variation
22. Graph Linear Functions
E. Writing Linear Equations (15 days)
23. Write Linear Equations in Slope-Intercept Form
24. Use Linear Equations in Slope-Intercept Form
25. Write Linear Equations in Point-Slope Form
26. Write Linear Equations in Standard Form
27. Write Equations of Parallel and Perpendicular Lines
28. Fit a Line to Data
29. Predict with Linear Models
F. Solving and Graphing Linear Inequalities (16 days)
30. Solve Inequalities Using Addition and Subtraction
31. Solve Inequalities Using Multiplication and Division
32. Solve Multi-Step Inequalities
33. Solve Compound Inequalities
34. Solve Absolute Value Equations
35. Solve Absolute Value Inequalities
36. Graph Linear Inequalities in Two Variables
G. Systems of Equations and Inequalities (15 days)
37. Solve Linear Systems by Graphing
38. Solve Linear Systems by Substitution
39. Solve Linear Systems by Adding or Subtracting
40. Solve Linear Systems by Multiplying First
41. Solve Special Types of Linear Systems
42. Solve Systems of Linear Inequalities
H. Exponents and Exponential Functions (17 days)
43. Apply Exponent Properties Involving Products
44. Apply Exponent Properties Involving Quotients
45. Define and Use Zero and Negative Exponents
46. Use Scientific Notation
47. Write and Graph Exponential Growth Functions
48. Write and Graph Exponential Decay Functions
I. Polynomials and Factoring (18 days)
49. Add and Subtract Polynomials
50. Multiply Polynomials
51. Find Special Products of Polynomials
52. Solve Polynomial Equations in Factored Form
53. Factor $x^{2}+b x+c$
54. Factor $\mathrm{ax}^{2}+\mathrm{bx}+\mathrm{c}$
55. Factor Special Products
56. Factor Polynomials Completely
J. Quadratic Equations and Functions (18 days)
57. Graph $y=a x^{2}+c$
58. Graphy $=a x^{2}+b x+c$
59. Solve Quadratic Equations by Graphing
60. Use Square Roots to Solve Quadratic Equations
61. Solve Quadratic Equations by Completing the Square
62. Solve Quadratic Equations by the Quadratic Formula
63. Interpret the Discriminant
64. Compare Linear, Exponential, and Quadratic Models
K. Radicals and Geometry Connections (10 days)
65. Graph Square Root Functions
66. Simplify Radical Expressions
67. Solve Radical Equations
68. Apply the Pythagorean Theorem and Its Converse
69. Apply the Distance and Midpoint Formulas
L. Rational Equations and Functions (14 days)
70. Model Inverse Variation
71. Graph Rational Functions
72. Divide Polynomials
73. Simplify Rational Expressions
74. Multiply and Divide Rational Expressions
75. Add and Subtract Rational Expressions
76. Solve Rational Equations
M. Probability and Data Analysis (13 days)
77. Find Probabilities and Odds
78. Find Probabilities Using Permutations
79. Find Probabilities Using Combinations
80. Find Probabilities of Compound Events
81. Analyze Surveys and Samples
82. Use Measures of Central Tendency and Dispersion
83. Interpret Stem-and-Leaf Plots and Histograms
84. Interpret Box-and-Whisker Plots
